Logic and the Methodology of Science

The Group in Logic and the Methodology of Science offers an interdisciplinary program of study and research leading to the PhD degree. Students in the program acquire a good understanding of the mathematical theory known as Mathematical Logic, which deals in a rigorous way with such central concepts as truth, definability, provability, and computability. They may then seek to contribute to this theory or to apply it. There are important areas of application in mathematics, philosophy, computer science, and elsewhere.

The program is administered by an interdepartmental group that cooperates closely with the Computer Science Division, the Department of Mathematics, and the Department of Philosophy.

Admission to the University

Minimum Requirements for Admission

The following minimum requirements apply to all graduate programs and will be verified by the Graduate Division:

1. A bachelor's degree or recognized equivalent from an accredited institution;
2. A grade point average of B or better (3.0);
3. If the applicant has completed a basic degree from a country or political entity (e.g., Quebec) where English is not the official language, adequate proficiency in English to do graduate work, as evidenced by a TOEFL score of at least 90 on the iBT test, 570 on the paper-and-pencil test, or an IELTS Band score of at least 7 on a 9-point scale (note that individual programs may set higher levels for any of these); and
4. Sufficient undergraduate training to do graduate work in the given field.

Applicants Who Already Hold a Graduate Degree

The Graduate Council views academic degrees not as vocational training certificates, but as evidence of broad training in research methods, independent study, and articulation of learning. Therefore, applicants who already have academic graduate degrees should be able to pursue new subject matter at an advanced level without the need to enroll in a related or similar graduate program.

Programs may consider students for an additional academic master's or professional master's degree only if the additional degree is in a distinctly different field.

Applicants admitted to a doctoral program that requires a master's degree to be earned at Berkeley as a prerequisite (even though the applicant already has a master's degree from another institution in the same or a closely allied field of study) will be permitted to undertake the second master's degree, despite the overlap in field.

The Graduate Division will admit students for a second doctoral degree only if they meet the following guidelines:

1. Applicants with doctoral degrees may be admitted for an additional doctoral degree only if that degree program is in a general area of knowledge distinctly different from the field in which they earned their original degree. For example, a physics PhD could be admitted to a doctoral degree program in music or history; however, a student with a doctoral degree in mathematics would not be permitted to add a PhD in statistics.
2. Applicants who hold the PhD degree may be admitted to a professional doctorate or professional master's degree program if there is no duplication of training involved.

Applicants may apply only to one single degree program or one concurrent degree program per admission cycle.

Required Documents for Applications

1. Transcripts: Applicants may upload unofficial transcripts with your application for the departmental initial review. Unofficial transcripts must contain specific information including the name of the applicant, name of the school, all courses, grades, units, & degree conferral (if applicable).
2. Letters of recommendation: Applicants may request online letters of recommendation through the online application system. Hard copies of recommendation letters must be sent directly to the program, by the recommender, not the Graduate Admissions.
3. Evidence of English language proficiency: All applicants who have completed a basic degree from a country or political entity in which the official language is not English are required to submit official evidence of English language proficiency. This applies to institutions from Bangladesh, Burma, Nepal, India, Pakistan, Latin America, the Middle East, the People's Republic of China, Taiwan, Japan, Korea, Southeast Asia, most European countries, and Quebec (Canada). However, applicants who, at the time of application, have already completed at least one year of full-time academic course work with grades of B or better at a US university may submit an official transcript from the US university to fulfill this requirement. The following courses will not fulfill this requirement:
   • courses in English as a Second Language,
   • courses conducted in a language other than English,
   • courses that will be completed after the application is submitted, and
   • courses of a non-academic nature.

Applicants who have previously applied to Berkeley must also submit new test scores that meet the current minimum requirement from one of the standardized tests. Official TOEFL score reports must be sent directly from Educational Test Services (ETS). The institution code for Berkeley is 4833 for Graduate Organizations. Official IELTS score reports must be sent electronically from the testing center to University of California, Berkeley, Graduation Division, Sproul Hall, Rm 318 MC 5900, Berkeley, CA 94720. TOEFL and IELTS score reports are only valid for two years prior to beginning the graduate program at UC Berkeley. Note: score reports can not expire before the month of June.

Where to Apply

Visit the Berkeley Graduate Division application page (http://grad.berkeley.edu/admissions/apply/).

Admission to the Program

For admission to the graduate program, students must have completed an undergraduate major in philosophy, mathematics, science, or some related field. Their course of study should include at least one full year
of upper division logic, one full year of upper division mathematics other
than logic, one full year of upper division philosophy, and one upper
division course in some science. Exceptions to these requirements are
permitted at the discretion of the head graduate adviser.

As in most PhD programs at Berkeley, the work in this program is
divided into two phases. In the first, the student acquires a fairly broad
but rigorous working knowledge in three areas. His or her competence
in these areas is tested in a two-part comprehensive preliminary
examination and a qualifying examination. Part I of the preliminary
examination deals with the foundations of mathematics (including
elements of model theory, recursion theory, and incompleteness and
undecidability results). Part II concerns one of the following areas of
philosophy: philosophy of science, philosophy of language, philosophy of
mathematics, or philosophical logic. The qualifying examination covers
material from a mathematics option, a philosophy option, or a special
option (for details, see Preliminary Examination (p. 2) and Qualifying
Examination (p. 3) below). Students are also required to take two
4-unit courses, Math 225A and 225B (Metamathematics), usually in
the first year of the program. In the second phase of the PhD program,
after having passed the qualifying examination, the student selects
a dissertation supervisor and, under his or her guidance, carries out
original research and writes a dissertation. Since most of the faculty have
strong interests in logic, students wishing to work in some other area of
the methodology of science may find difficulty in finding a dissertation
supervisor unless they propose to approach their problems using the
methods of mathematics and logic.

Advancement to Candidacy

For advancement to candidacy for the PhD degree, the student must
complete the requirements described in Independent Work (p. 2),
Preliminary Examination (p. 2), and Qualifying Examination
(p. 3), below, and must arrange for a faculty member of the group
to serve as his or her dissertation supervisor.

Independent Work

Each student must give evidence of capacity to work independently.
As regards philosophy, each student must successfully complete a
one-semester long philosophy seminar. The seminar must call for the
student’s active participation, involving both (i) the oral exposition of
assigned papers and topics and (ii) the completion of a term paper. This
requirement is to be completed prior to the appointment of the committee
for the qualifying examination. As regards mathematics, each student
who chooses the mathematics option of the qualifying examination must
take a course or seminar in mathematics that involves the oral exposition
of assigned papers and topics.

Preliminary Examination

The preliminary examination consists of two separate parts, which are
usually taken on different days. The two parts can be taken in any order,
however, Part II may only be taken after passing the philosophy seminar
requirement.

Part I. This is a three hour written examination in the foundations of
mathematics covering roughly the standard topics usually included in
MATH 225A /MATH 225B (Metamathematics). The foundations exam is
given once a year, usually in June. An additional exam may be offered
in December. Logic graduate students are required to take these two
courses for credit, which is usually done in the student’s first year in
the program. Exceptions to this course requirement may be granted by
petition.

Sample topics include (but are not limited to) the following:

• **First-order logic:** Completeness theorem, compactness theorem,
preservation theorems, Löwenheim-Skolem theorems, complete
theories, decidable theories. Elementary and pseudo-elementary
classes, elementary equivalence and elementary extensions, Skolem
functions, characterization of universal classes, interpolation and
Beth’s definability theorem. Applications such as dense linear
orderings and algebraically closed fields.

• **Incompleteness and undecidability:** Recursive and recursively
enumerable sets, the arithmetic hierarchy. Interpretability between
theories. Applications to undecidability of theories. Gödel’s
incompleteness theorem. Formalized arithmetic and Gödel’s theorem
on consistency proofs.

Students are expected to be fully conversant with basic notions in logic
at the level of an undergraduate mathematical logic courses as exposed
in textbooks such as Enderton’s “A Mathematical Introduction to Logic.”
Students are not expected to have expertise in set theory, but they
should understand it somewhat beyond the undergraduate level (as
represented, for example, in Enderton’s “Elements of Set Theory”). The
first part (through chapter 13 on the constructible universe) of Jech’s “Set
Theory” contains the requisite material. For recursion theory, Soare’s
book “Recursively Enumerable Sets and Degrees” through parts A and
B is a good reference. For Gödel’s incompleteness theorems and the
theory of Peano arithmetic, Kaye’s book “Models of Peano Arithmetic”
is an excellent source. For model theory, there are several good books,
al of which bear slight variants of the title “Model Theory” by Chang
and Keisler, Hodges, Marker, and Poizat.

It is important to recognize that these texts include material which goes
beyond what would be expected on the preliminary examination. On
the other hand, the questions for the examination will not be derived
exclusively from these sources. Students should consult with the
committee in charge of the preliminary examination during the preceding
semester for advice about a more detailed preparatory course of study
and readings.

Past examinations are archived online (http://logic.berkeley.edu/past-
prelims.html).

**Part II.** This is a three hour written examination in one of the following
fields:

• Philosophy of mathematics and logic
• Philosophical logic (broadly construed to include formal epistemology,
probability, decision theory, and game theory)
• Philosophy of science
• Philosophy of language

A student may take this part of the preliminary examination only
after completing the philosophy seminar requirement as described in
Independent Work (p. 2). Students may wish to take an independent
study course with a Logic Group philosophy professor to prepare for
this part of the examination, and this can be done concurrently with the
philosophy seminar. Other resources for preparing for the examination
include upper division undergraduate courses and graduate seminars
which the Philosophy Department regularly offers in all of these fields.
The student’s plan of study must be within one of the four areas listed, and must be agreed to by the examination committee well before the date is set for the examination. An archive of preapproved syllabi, some of which coordinate with course offerings in the Philosophy Department, is available here (http://logic.berkeley.edu/philosophy-prelims.html). A student may wish instead to submit a prospectus for a special course of study, which would include a list of readings and a brief description of the topics to be covered in the examination. This option requires approval of the committee.

Procedural Matters

For Part I: A three-member examining committee will be appointed by the Chair of the Group in Logic and the Methodology of Science to administer the first part of the preliminary examination. The chair of the committee must be a member of the group. The date of the examination will be set by the chair of the group. This examination will usually be offered only once each academic year, in June. If in a given year it is deemed necessary, an additional examination will be scheduled for January.

For Part II: A (second) three-member examining committee will be selected by the student subject to approval by the Chair of the Group in Logic and the Methodology of Science. This committee must consist of at least two members of the Philosophy Department, and the chair of the committee must be a member of the group. The examination date may be chosen by the student, subject to the approval of the chair of the committee. The committee will prepare a list of six questions that shall constitute the written exam. The examination will be graded by the committee members on a pass/non-pass basis.

If in any of the two parts of the preliminary examination the student is deemed to have failed that part on the first try, the student may request re-examination. A third attempt, for either part, is not permitted. A student failing any part of the preliminary examination must consult promptly with the graduate adviser.

Qualifying Examination

The oral qualifying examination is held on one day and is normally two to three hours in length. For the qualifying examination the student may choose one of the following three options; no matter which option is chosen, the Graduate Council requires that three subject areas be entered on the application for the qualifying examination that is due in the Graduate Division for processing at least three weeks before the exam.

Mathematics Option

The oral qualifying examination is held on one day and is normally two to three hours in length. At last three subject areas must be covered during the examination. The student may select either all of the material in analysis and about half of the material in algebra (either general algebra, groups, and rings or general algebra, vector spaces and modules, and fields) or all of the material in algebra and about half of the material in analysis (either general topology or measure and integration).

Analysis

• General topology: Metric spaces, completeness. Topological spaces, bases, continuous functions, subspaces, product spaces, quotient spaces. Connectedness, separability, Hausdorff spaces. Compactness and Tychonov’s theorem. Subspaces and continuous functions for compact spaces. Zero-dimensional spaces and Stone’s representation theorem for Boolean algebras. Meager sets, property of Baire, Baire category theorem, and the Kuratowski-Ulam theorem. Convergence of nets. This material can be found in Royden (Sections 2.7, Chapters 7-8, and Sections 9.1-9.6) and Oxtoby (Chapters 1, 4, 8, 9, 12, 15). Much of the material can also be found in the corresponding parts of Chapters 1, 2, 3, 5 of Kelley, in expanded form in Munkres, and in advanced form in Dugundji. Most (but not quite all) of the material is normally covered in MATH 202A (Topology and Analysis).

• Measure and integration: Lebesgue measure and integration in Rn. Construction of measure and integral. Monotone convergence, dominated convergence, absolute continuity, Radon-Nikodým theorem, Fubini’s theorem, Egorov’s theorem. Elements of general measure and integration theory. Borel spaces. Product measures. This material can be found in Rudin (Chapter 11 through p. 325), Bartle (Chapters 1-5, 7-8, 10), and Oxtoby (Chapters 1, 3, 8). Much of the material can also be found in Royden (Chapters 3-4 and Sections 11.1-11.6), Halmos (parts of Chapters 1-7), and Burkill. Most (but not quite all) of the material is normally covered in MATH 105 (Second Course in Analysis).

Algebra

• General algebra: Subalgebras, homomorphisms, congruences, and quotient algebras. Direct and subdirect products, free algebras and varieties. The material can be found in Grätzer (Chapters 7, 11, 19, and Jacobson (Section 1.11). Some of the material can also be found in Malcev (Section 2).

• Groups: Permutation and alternating groups. Normal subgroups, abelian groups and finitely generated abelian groups. Sylow theorems. The material can be found in Herstein (Sections 1.3, 2.1-2.11, 2.13-2.14). The material can also be found in Jacobson (Sections 1.1-1.12), Rotman (Chapters 1-4 through p. 60), and Sah (Chapters III 1, 2, 4, 5).

• Rings: Ideals and quotient rings, integral domains, Euclidean rings, polynomial rings, unique factorization domains. The material can be found in Herstein (Chapter 3). The material can also be found in Sah (Chapter IV), Zariski-Samuel (parts of Chapter I), and Lang (Chapters I and V).

• Vector spaces and modules: Basic concepts. Linear independence and bases. Modules. The material can be found in Herstein (Sections 4.1, 4.2, 4.5). The material can also be found in Sah, Zariski-Samuel, and Lang.

• Fields: Algebraic extensions, splitting field, separable extensions, basic ideas of Galois theory, transcendental extensions and degree of transcendence, real closed and algebraically closed fields. The material can be found in Herstein (Sections 5.1, 5.3-5.8) and van der Waerden (Sections 62-64, 66-71).

Philosophy Option

An oral examination in a field chosen from one of the four areas listed under Part II above, or (with permission from the graduate adviser) from some other area of philosophy. The graduate adviser must judge the scope and the intended reading list to be sufficiently different from that of the student’s Part II examination. The exam must conform to the university rules and regulations for qualifying examinations. In particular, the examination must cover at least three topics.

Special Option

A special examination based on the needs of the individual student. In this case the student must submit a proposed syllabus and then obtain
written approval of the graduate adviser and a faculty member of the
group (who thereby expresses willingness to become the student’s
dissertation supervisor); such approval is only to be given after circulation
of the student’s proposal among all group faculty members for comment.
The exam must conform to the university rules and regulations for
qualifying examinations. In particular, the examination must be an oral
examination covering at least three topics.

**Procedural Matters**

For the qualifying examination, a four-member examining committee will
be appointed by the dean of the Graduate Division upon recommendation
of the graduate adviser. Committee members must be members of
Berkeley’s Academic Senate and the Chair must be a member of the
Logic Group.

For the philosophy option of qualifying examination, the student must
submit to the examination committee a prospectus outlining the scope
of the oral examination. The prospectus should include a reading list
and a brief description of the topics to be covered in the examination.
Prior to approval of the prospectus, the chair of this committee may
consult with the faculty member of the Department of Philosophy who
is in charge of the department’s qualifying examination concerning the
reading list and topics to be covered. (If the prospectus submitted is
judged to be acceptable by the committee, a copy will be put in a file in
the group office for purposes of guiding other students and examination
committees.) The prospectus should be submitted to the committee well
in advance of the examination date. If the student is judged to have failed
the qualifying examination on the first try, the committee may recommend
that the student be granted a reexamination following a reasonable
delay, usually of three months. A third attempt is not permitted. A student
failing the qualifying examination must consult promptly with the graduate
adviser.

**Dissertation and Final Examination**

After advancement to candidacy, the student must write an acceptable
dissertation and pass a final oral examination in order to earn the degree.
In administering this requirement the group follows Plan A as outlined
in the Berkeley Academic Guide in the section entitled “The Doctoral
Dissertation.”

**Time Limits**

The Graduate Division together with the group has imposed the following
requirements to help regulate the progress of students in the program
 toward the PhD.

Each student must 1) pass both parts of the preliminary examination
before the beginning of the fifth semester, 2) attempt one of them before
the beginning of the third semester, and 3) attempt both of them before
the beginning of the fourth semester. Permission for an extension of
these time limits will only be granted in special circumstances and
requires the written permission of the chair and graduate advisor.

Each student must pass the qualifying examination within three calendar
years after entering the program, again unless explicit written permission
is granted by the chair and graduate adviser for an extension of this time
limit.

These are maximum time limits. All students are encouraged to take both
parts of the preliminary examination and the qualifying examination as
soon as possible and in fact, many students will take them much sooner
than required by the time limits given above. (The graduate advisor can
in individual cases, e.g., for students entering with relevant prior graduate

study at Berkeley or elsewhere, insist that the examinations be taken
within stricter time limits.) Students must be advanced to candidacy
for the PhD no later than the semester following the one in which the
qualifying examination was passed.

Students must complete all requirements for the PhD degree within four
years after advancement to candidacy. Students who do not obtain the
PhD within this four-year period will no longer be considered in candidacy
for the PhD unless special action is taken by the group.